

# Quick Guide to Fractions

**Fractions** are another way of expressing division. The expression  $12/3$  is equal to 4 because 12 divided by 3 is 4. If you don't believe me, check that  $3 * 4 = 12$ ; that's an **equivalent** statement.

Now you have your **proper fractions**, where the **numerator** (top) is smaller than the **denominator** (bottom), like  $5/12$ . These give numbers that are less than 1.

On the other hand, there are **improper fractions** like  $19/8$ . Think of pizzas each cut into eight slices; each slice is one eighth, or  $1/8$  of a pizza. Then 19 slices would be the same as 16 slices and 3 more slices; making 2 pizzas and 3 extra slices.

Therefore we get  $19 / 8 = 2 + 3/8$ , which is written as  $2 \frac{3}{8}$ , called a **mixed number**.

To convert  $19/8$  you do division; 8 into 19 goes 2 times with 3 left over; so  $2 \frac{3}{8}$ .

If you have a mixed number like  $3 \frac{1}{7}$ , you do the reverse:  $3 * 7 + 1 = 22$ ; so  $22/7$ .

Some misguided people (not you!) think that pi is equal to  $3 \frac{1}{7}$ ; it's merely close. Pi is an **irrational number**, which means it's a real number, but not equal to any fraction. (But  $355/113$  is closer to pi.)

**Fractions** can be put into lowest terms, meaning you cancel out common factors of the top & bottom.

*For example,  $6 / 8 = (2*3) / (2*4) = 3 / 4$ ; six eighths equals three fourths.*

Examples of **fraction operations**:

**Multiplying:**

$$(3/4) * (5/6) = (3*5) / (4*6) = 15 / 24 = 5/8 \text{ (in lowest terms.)}$$

**Dividing :**

$$(3/4) / (5/6) = (3/4) * (6/5) = 18 / 20 = 9/10 \text{ (invert and multiply)}$$

**Adding :**

$$(3/4) + (5/6) = (9/12) + (10/12) = (9+10)/12 = 19/12 = 1 \frac{7}{12} \text{ (common denominator)}$$

