

The Difference/Sum of Cubes

$$\text{Formulas} : \quad x^3 - y^3 = (x - y)(x^2 + xy + y^2)$$

$$x^3 + y^3 = (x + y)(x^2 - xy + y^2)$$

Examples : $x^3 - 27$

$$\begin{aligned} &= x^3 - 3^3 \\ &= (x - 3)(x^2 + 3x + 3^2) \end{aligned}$$

*break down to cubes
factor using formula*

$$\begin{aligned} 27x^3 + 8y^3 &= 3^3 x^3 + 2^3 y^3 \\ &= (3x + 2y)(3^2 x^2 - (2x)(3y) + 2^2 y^2) \\ &= (3x + 2y)(9x^2 - 6xy + 4y^2) \end{aligned}$$

*break down to cubes
factor using formula*

$$\begin{aligned} x^6 - 64 &= x^6 - 2^6 \\ &= (x^2)^3 - (2^2)^3 \\ &= [(x^2) - (2^2)][(x^2)^2 + (x^2)(2^2) + (2^2)^2] \\ &= (x^2 - 2^2)(x^4 + 4x^2 + 16) \\ &= (x + 2)(x - 2)(x^4 + 4x^2 + 16) \end{aligned}$$

*break down to exponents
break down into cubes
use formula*

why?

$$\begin{aligned} 8x^3 + 27y^3 &= 2^3 x^3 + 3^3 y^3 \\ &= (2x + 3y)(2^2 x^2 - (2x)(3y) + 3^2 y^2) \\ &= (2x + 3y)(4x^2 - 6xy + 9y^2) \end{aligned}$$

*break down to cubes
use formula*

$$\begin{aligned} x^6 + 64 &= x^6 + 2^6 \\ &= (x^2)^3 + (2^2)^3 \\ &= [(x^2) + (2^2)][(x^2)^2 - (x^2)(2^2) + (2^2)^2] \\ &= (x^2 + 4)(x^4 - 4x^2 + 16) \end{aligned}$$

*break down to exponents
break down to cubes
use formula*